

# New Initialisation Techniques for Multi-Objective Local Search

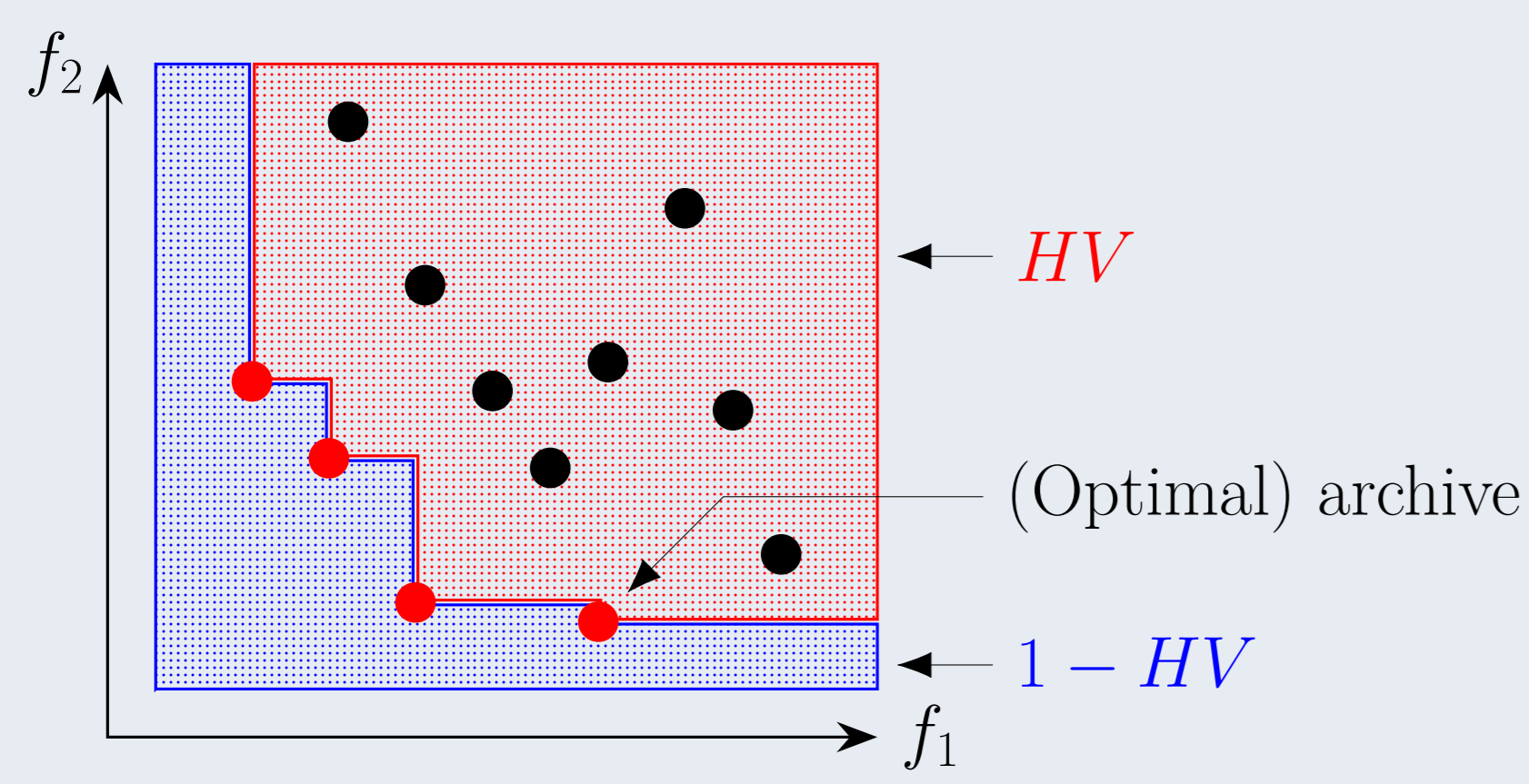
## Application to the Bi-Objective Permutation Flowshop

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### Multi-Objective Optimisation



### Multi-Objective Local Search

#### Taxonomy

SBLS: **scalarisation**-based local search

- Aggregate the criteria to a single one
- Use a single-objective local search

DBLS: **dominance**-based local search

- Use Pareto dominance

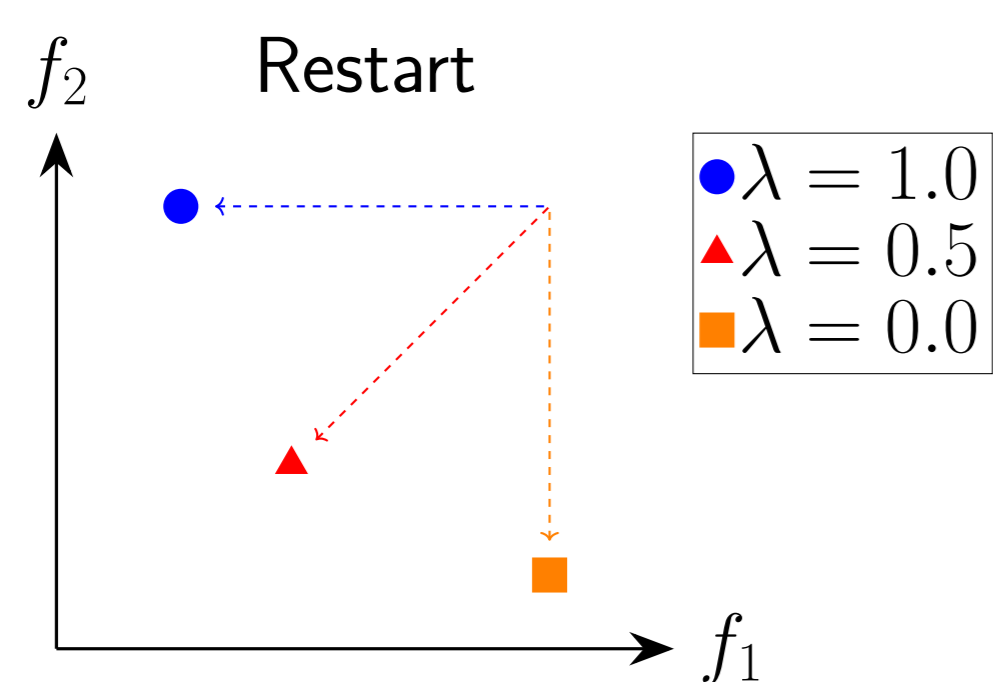
#### State of the art

- SBLS as initialisation procedure
- DBLS as main algorithm

### Known SBLS Strategies

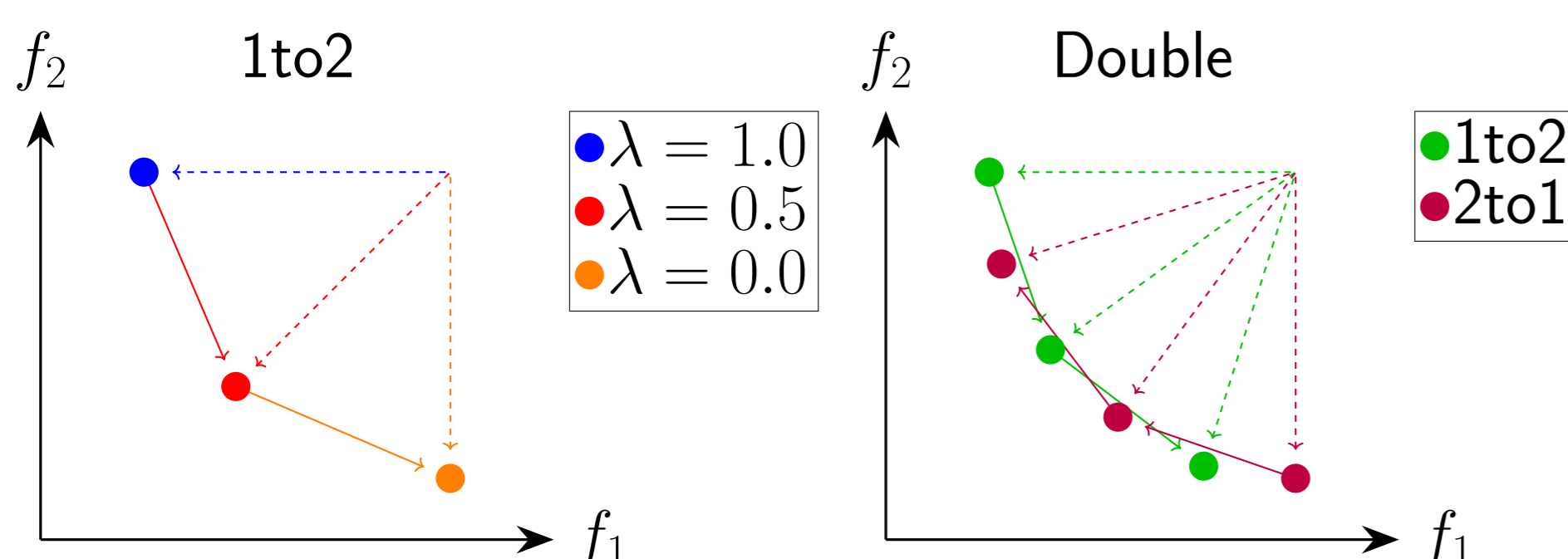
#### Restart

Divide the search in independent scalar problems



#### 1to2, 2to1, Double

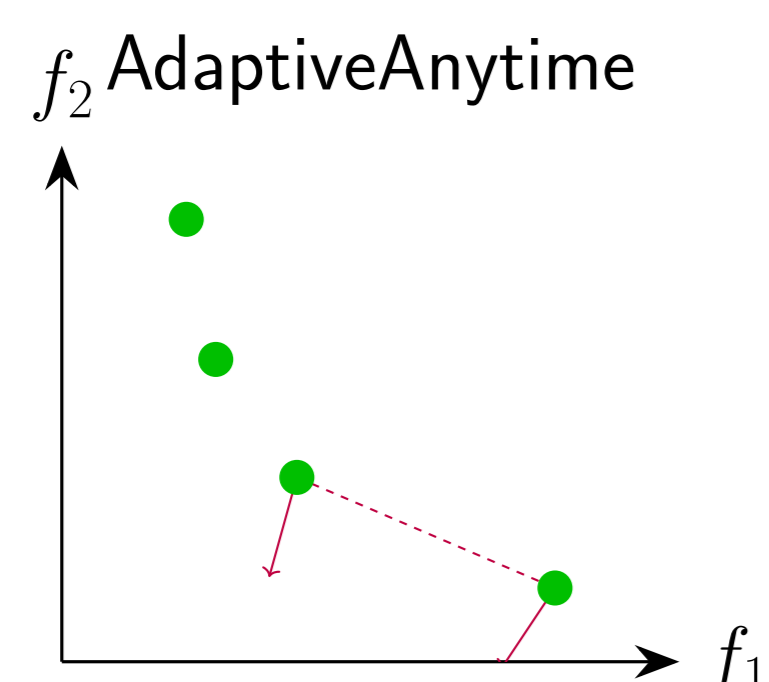
Re-use final solutions as initial solutions



#### AdaptiveAnytime [1]

Adapt the scalarisations during the search

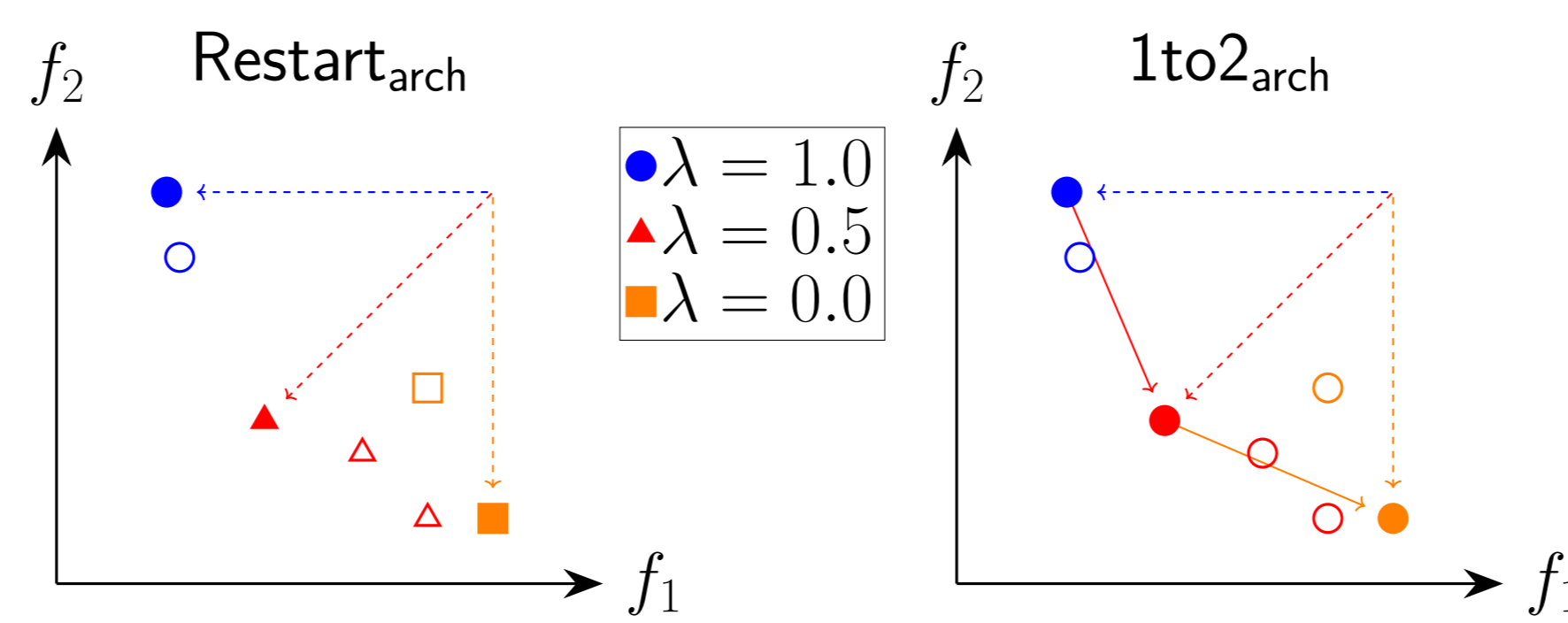
Target the biggest gap in the archive



### Archive-aware Variants

#### Restart<sub>arch</sub>, 1to2<sub>arch</sub>, 2to1<sub>arch</sub>, Double<sub>arch</sub>

Final archives are merged; trajectories are conserved



#### AdaptiveAnytime<sub>arch</sub>

Archives are merged every time: trajectories are affected

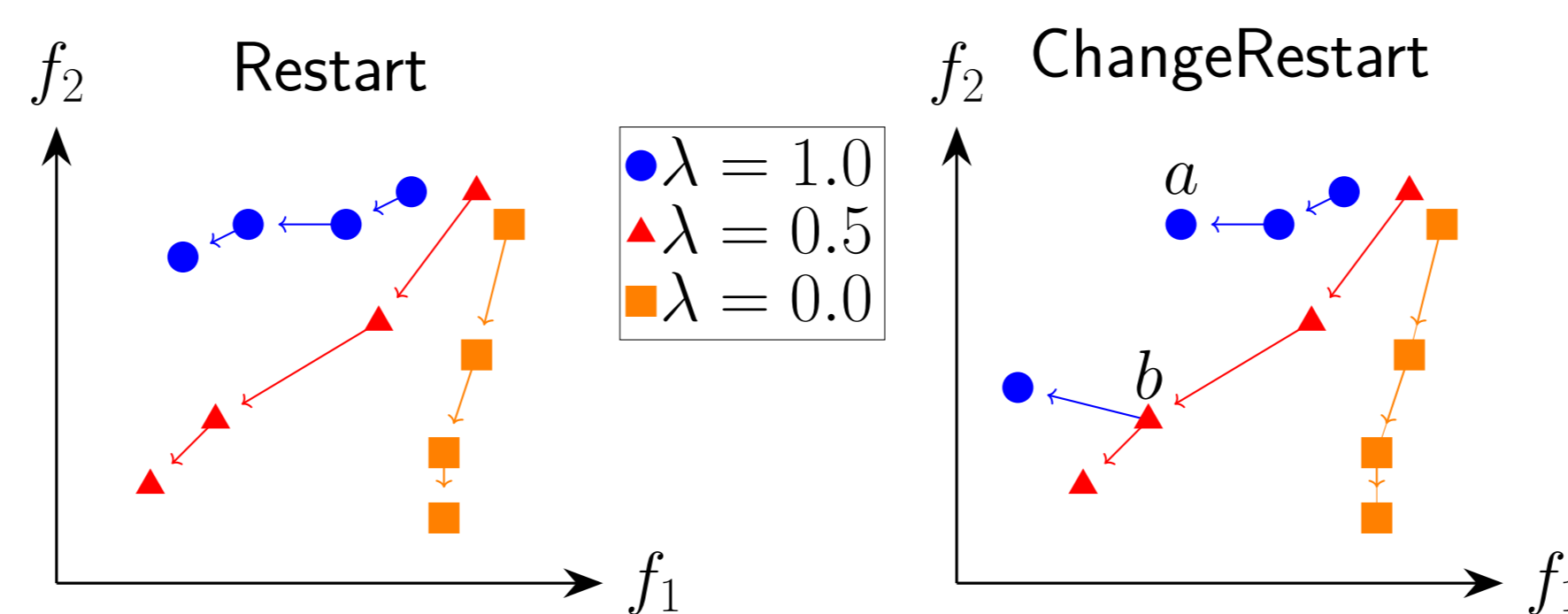
### New SBLS Strategies

#### ChangeRestart

Based on Restart

Break the search into smaller chunks

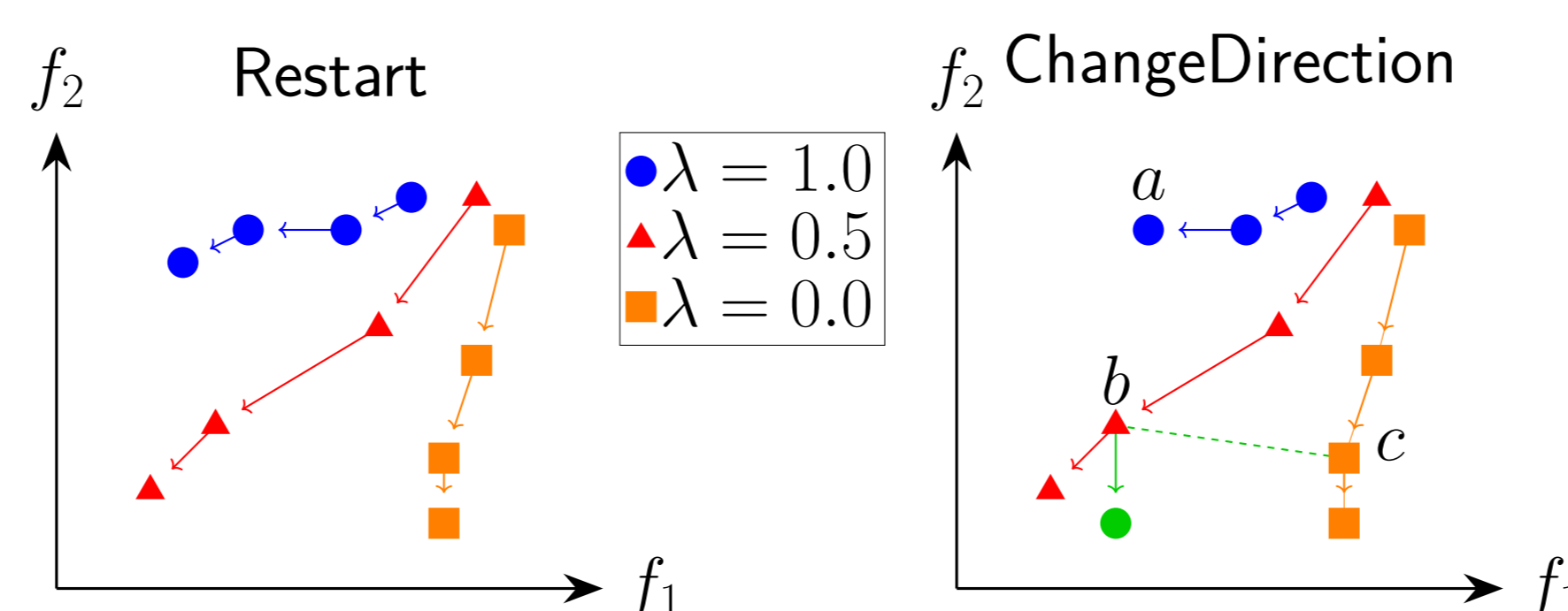
Stop dominated directions



#### ChangeDirection

Based on ChangeRestart

Continue based on the biggest gap (AdaptiveAnytime)



#### ChangeRestart<sub>arch</sub>, ChangeDirection<sub>arch</sub>

Intermediary archives are merged: trajectories are affected

### Experimental Setup

#### Problem

Bi-objective permutation flowshop scheduling problem

- makespan
- total flowtime

8 classes of Taillard PFSP instances [2]

- 20, 50, 100, 200 jobs
- 10, 20 machines

#### Algorithm

- 25% initialisation (NEH+IG [3])
- 75% multi-objective local search (iterated PLS [1, 4])

#### Protocol

- 12 SBLS strategies
- 50 runs per PFSP instance class (400 runs)

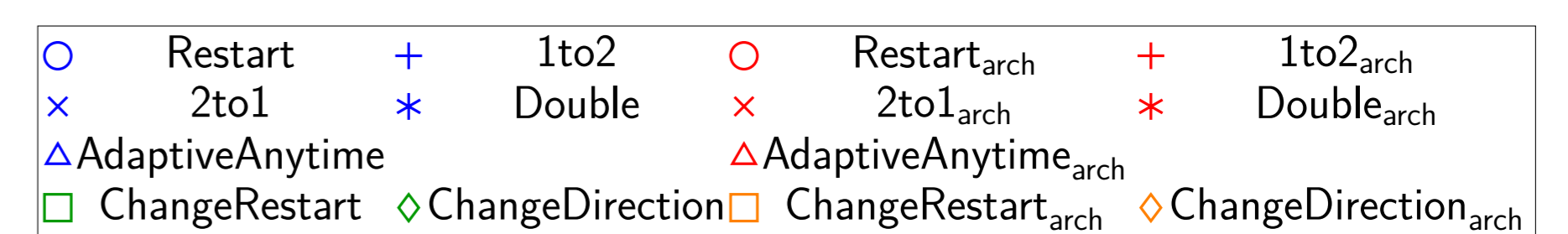
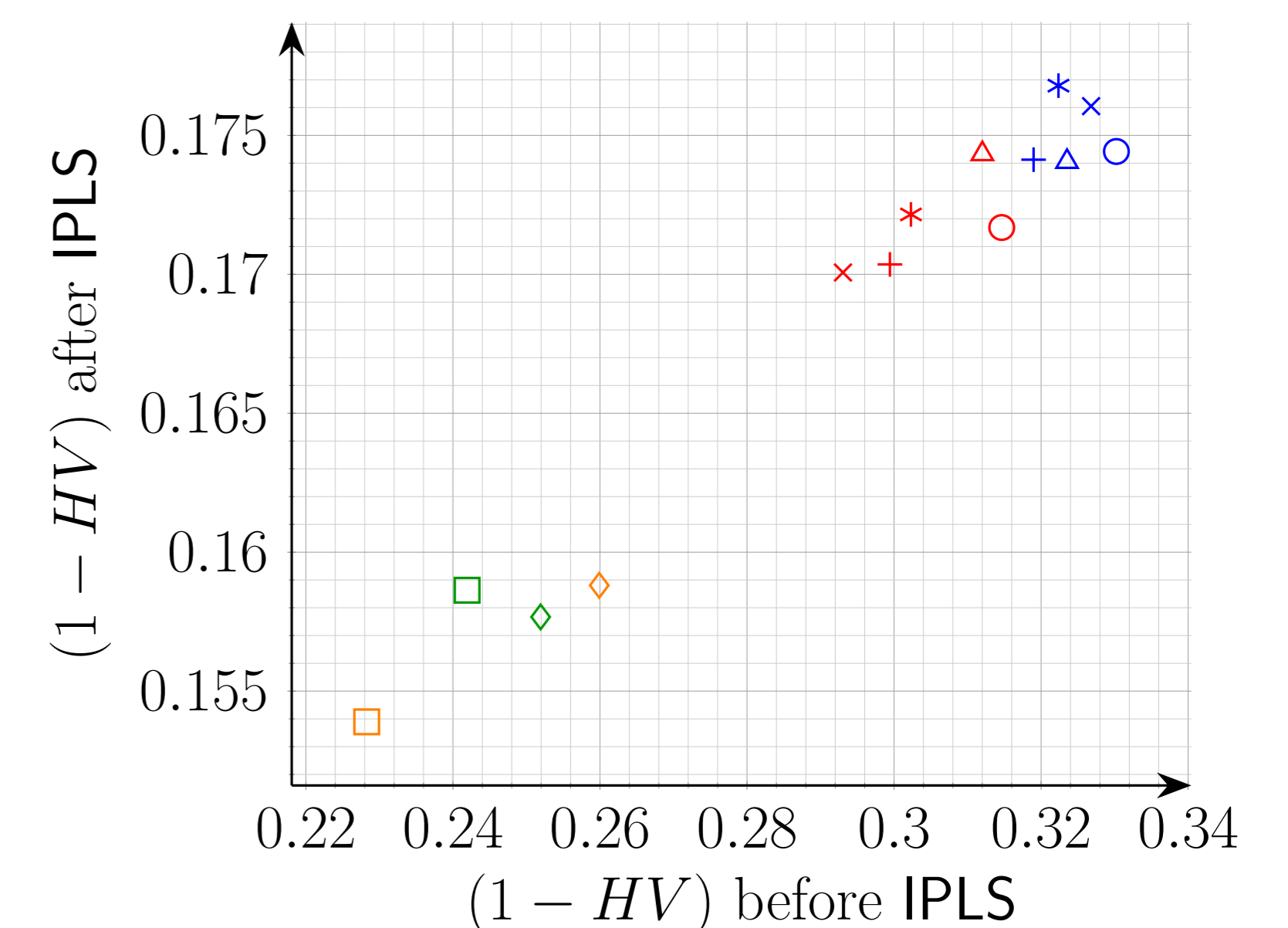
Table 1: SBLS parameter values

	$N^{\text{scalar}}$	$N^{\text{steps}}$	$T^{\text{first}}$	$\theta$
Restart	12			
1to2	12		1.5	
2to1	12		1.5	
Double	12		1.5	
AdaptiveAnytime	12		1.5	0.25
ChangeRestart	12	20	1.5	
ChangeDirection	12	20	1.5	0.25

### Results

#### Performance Assessment

- Before IPLS: to compare SLBS strategies
- After IPLS: to validate final results



### Statistical Analysis after IPLS

Wilcoxon test ("✓" means rank 1)

	Restart	1to2	2to1	Double	AdaptiveAnytime	Restart <sub>arch</sub>	1to2 <sub>arch</sub>	2to1 <sub>arch</sub>	Double <sub>arch</sub>	AdaptiveAnytime <sub>arch</sub>	ChangeRestart	ChangeRestart <sub>arch</sub>	ChangeDirection	ChangeDirection <sub>arch</sub>
20 × 10					✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
20 × 20					✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
50 × 10		✓			✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
50 × 20		✓	✓		✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
100 × 10					✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
100 × 20		✓			✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
200 × 10					✓	✓	✓	✓	✓	✓	✓	✓	✓	✓
200 × 20					✓	✓	✓	✓	✓	✓	✓	✓	✓	✓

### Summary

#### Results

- Archive-aware SBLS perform better
- New SBLS are almost never outperformed

#### Conclusions

- Single-objective sub-problems benefit from multi-objective knowledge
- Intermediary solutions should not be discarded

#### Future Work

- In-depth study of parameter interactions
- Archive-aware SBLS validation on other problems

### References

- [1] Jérémie Dubois-Lacoste, Manuel López-Ibáñez, and Thomas Stützle. Improving the anytime behavior of two-phase local search. *Annals of Mathematics and Artificial Intelligence*, 61(2):125–154, 2011.
- [2] Éric D. Taillard. Benchmarks for basic scheduling problems. *European Journal of Operational Research*, 64(2):278–285, 1993.
- [3] Rubén Ruiz and Thomas Stützle. A simple and effective iterated greedy algorithm for the permutation flowshop scheduling problem. *European Journal of Operational Research*, 177(3):2033–2049, 2007.
- [4] Aymeric Blot, Laetitia Jourdan, and Marie-Éléonore Kessaci. Automatic design of multi-objective local search algorithms: case study on a bi-objective permutation flowshop scheduling problem. In *Proceedings of the Genetic and Evolutionary Computation Conference, GECCO 2017*, pages 227–234. ACM Press, 2017.

### This Poster in a Nutshell

#### Observation

- SBLS benefit from multi-objective knowledge

#### Aims

- Augment SBLS with archives
- Propose new SBLS strategies
- Overall, improve SBLS+DBLS results